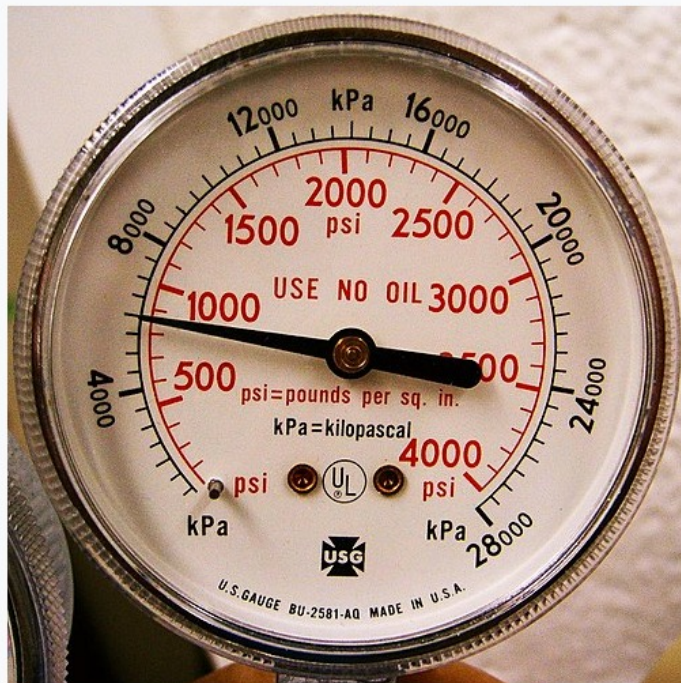


What is pressure?

# Pressure: Force per unit Area Energy per unit Volume

pascal



A pressure gauge reading in psi (red scale) and kPa (black scale)

Unit system	SI unit
Unit of	Pressure or stress
Symbol	Pa
Named after	Blaise Pascal
Conversions	
1 Pa in ...	... is equal to ...
SI base units:	$\text{kg}\cdot\text{m}^{-1}\cdot\text{s}^{-2}$
US customary units:	$1.450 \times 10^{-4}$ psi
atmosphere:	$9.869 \times 10^{-6}$ atm
bar:	$10^{-5}$ bar

Scalars (do not have direction or “components”):

Temperature  
Pressure  
Speed

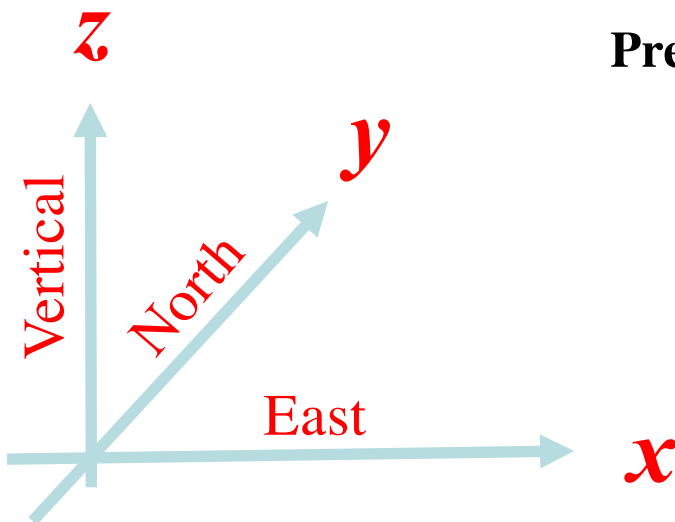
Vectors (have direction and “components”):

**Position** with components East (x), North (y), Vertical (z)

**Velocity** with components East (u), North (v), and Vertical (w)

**Force** with components East ( $F_x$ ), North ( $F_y$ ), and Vertical ( $F_z$ )

**Pressure Gradient** with components



in x-direction:

in y-direction:

in z-direction:

pressure change in x-direction

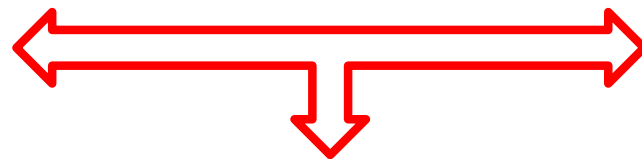
pressure change in y-direction

pressure change in z-direction

# Balance of Forces (Newton, 1687):

$$\text{Sum of Applied Forces} = \text{Mass} * \text{Acceleration}$$

acceleration is the time rate of change of velocity  
velocity is the time rate of change of location



Calculus

# Balance of Forces (Newton, 1687):

Simple Example:

(acceleration=0)

$$\begin{aligned}\text{Sum of Applied Forces} &= 0 \\ \text{Force1} + \text{Force2} &= 0\end{aligned}$$

Force1: Gravity

Force2: Pressure Difference (gradient)



Low P

High P

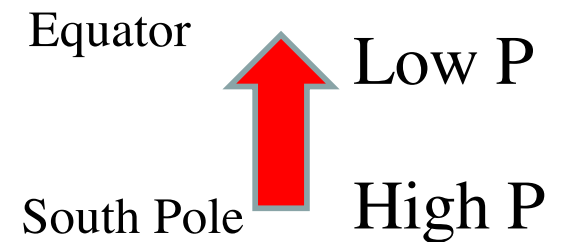
# Mermaid Movie

# Balance of Forces (Newton, 1687):

Simple Example:  
(acceleration  $\neq 0$ )

Sum of Applied Forces = mass \* acceleration  
Force2 = mass \* acceleration

Force2: Pressure Difference (gradient)



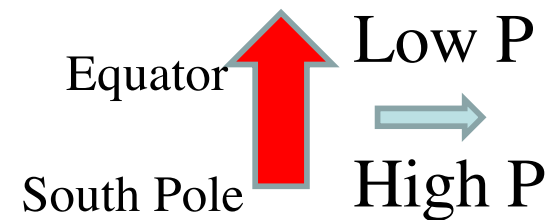
# Balance of Forces (Newton, 1687):

Example:  
(Coriolis)

Sum of Applied Forces = mass\*acceleration  
Force2+Force3 = mass\*acceleration

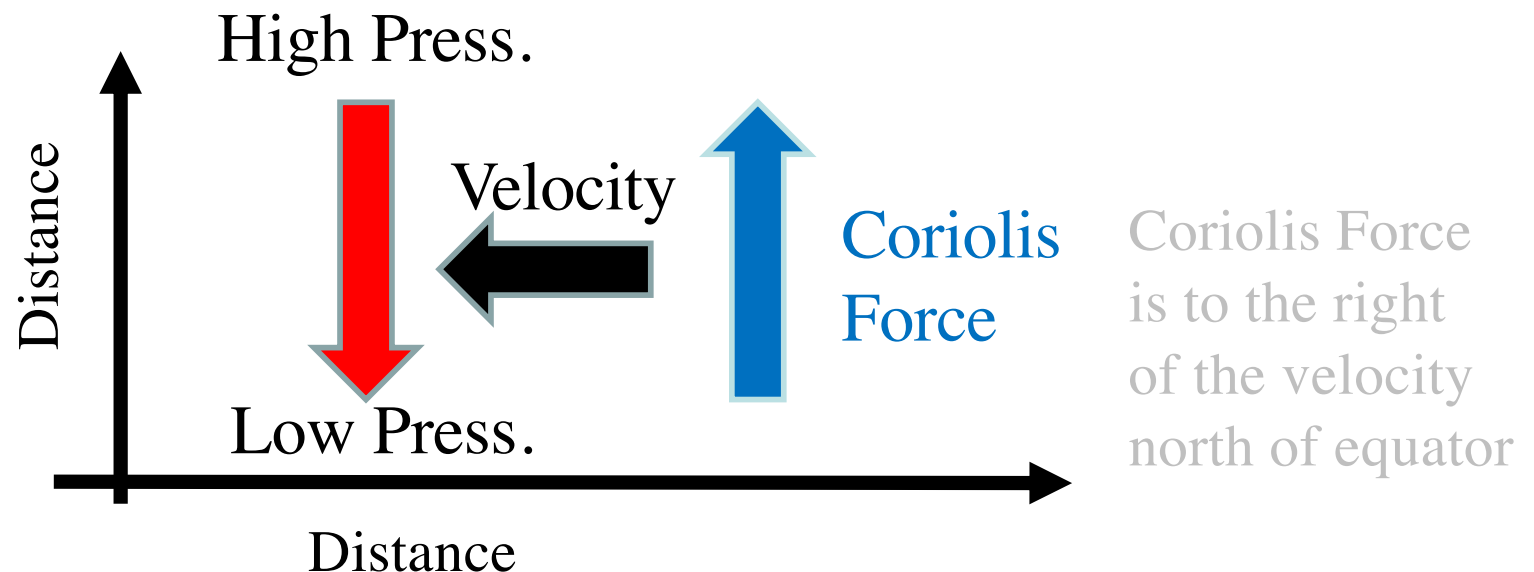
Force2: Pressure Difference (gradient)

Force3: Coriolis



Sum of Applied Forces = mass\*acceleration

$$\text{Force1} + \text{Coriolis Force} = 0$$



$$\text{Sum of Applied Forces} = \text{mass} * \text{acceleration}$$
$$\text{Force1} + \text{Coriolis} + \text{Force3} = 0$$

Force1: Pressure Gradient

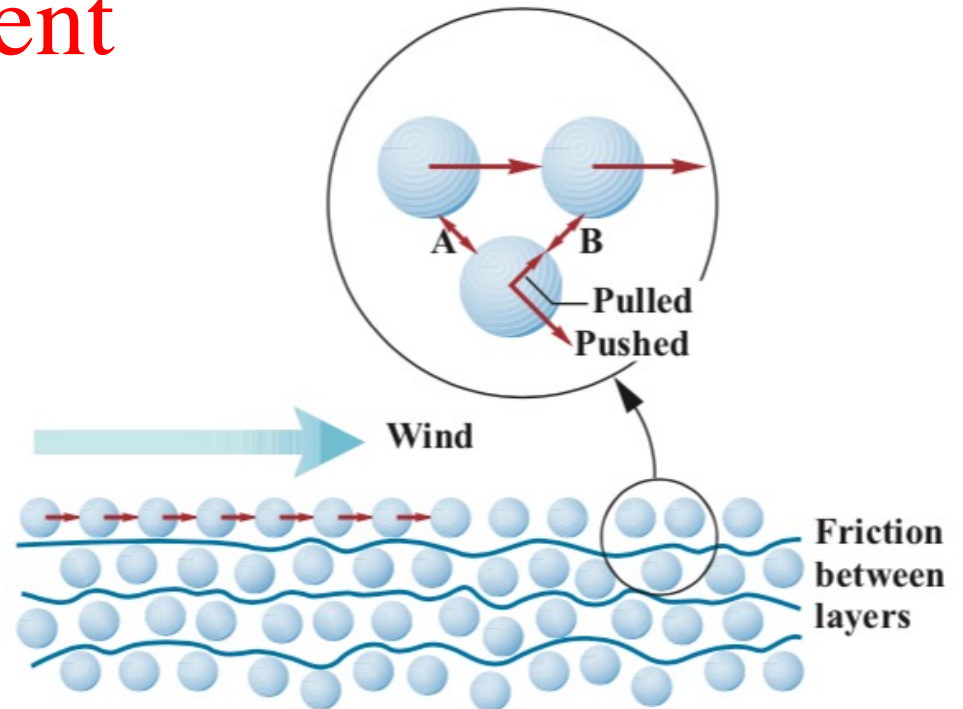
Force2: Coriolis

Force3: Friction

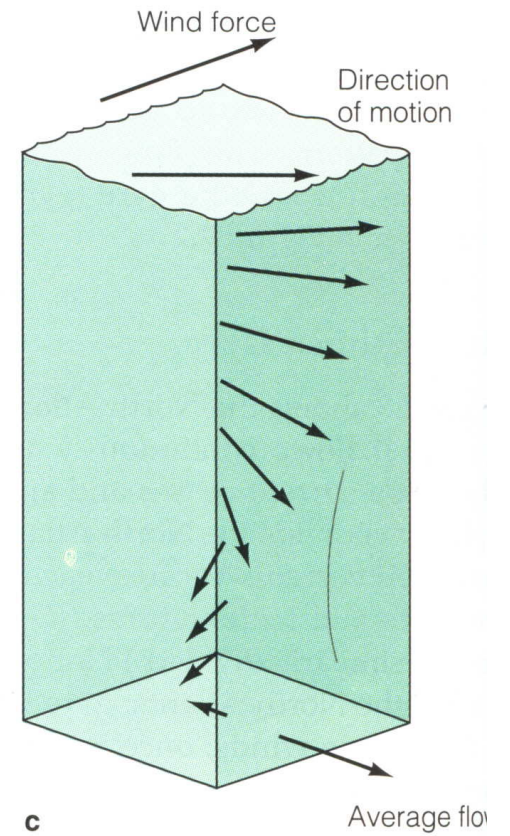
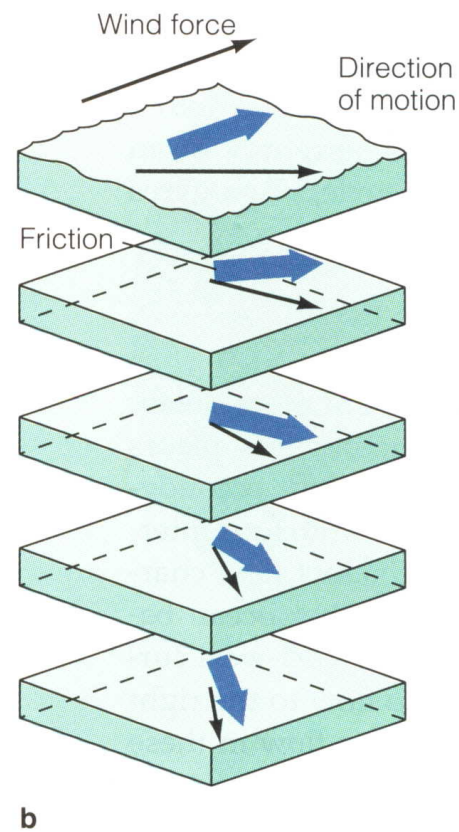
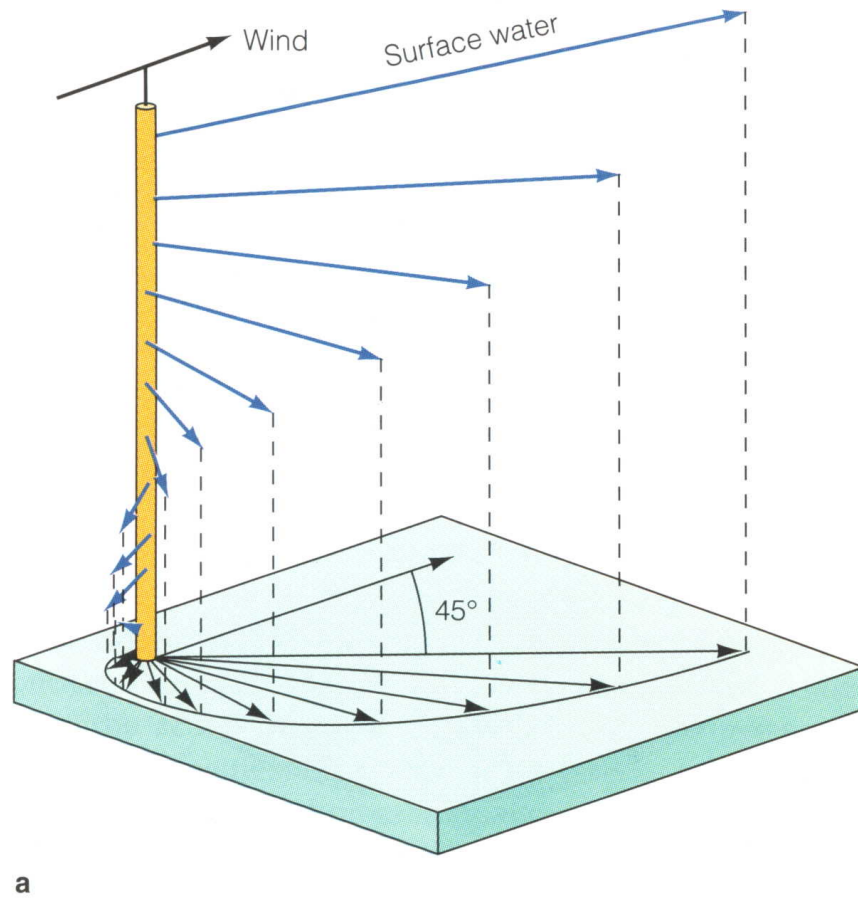
1+2 = Geostrophic Dynamics

2+3 = Ekman Dynamics

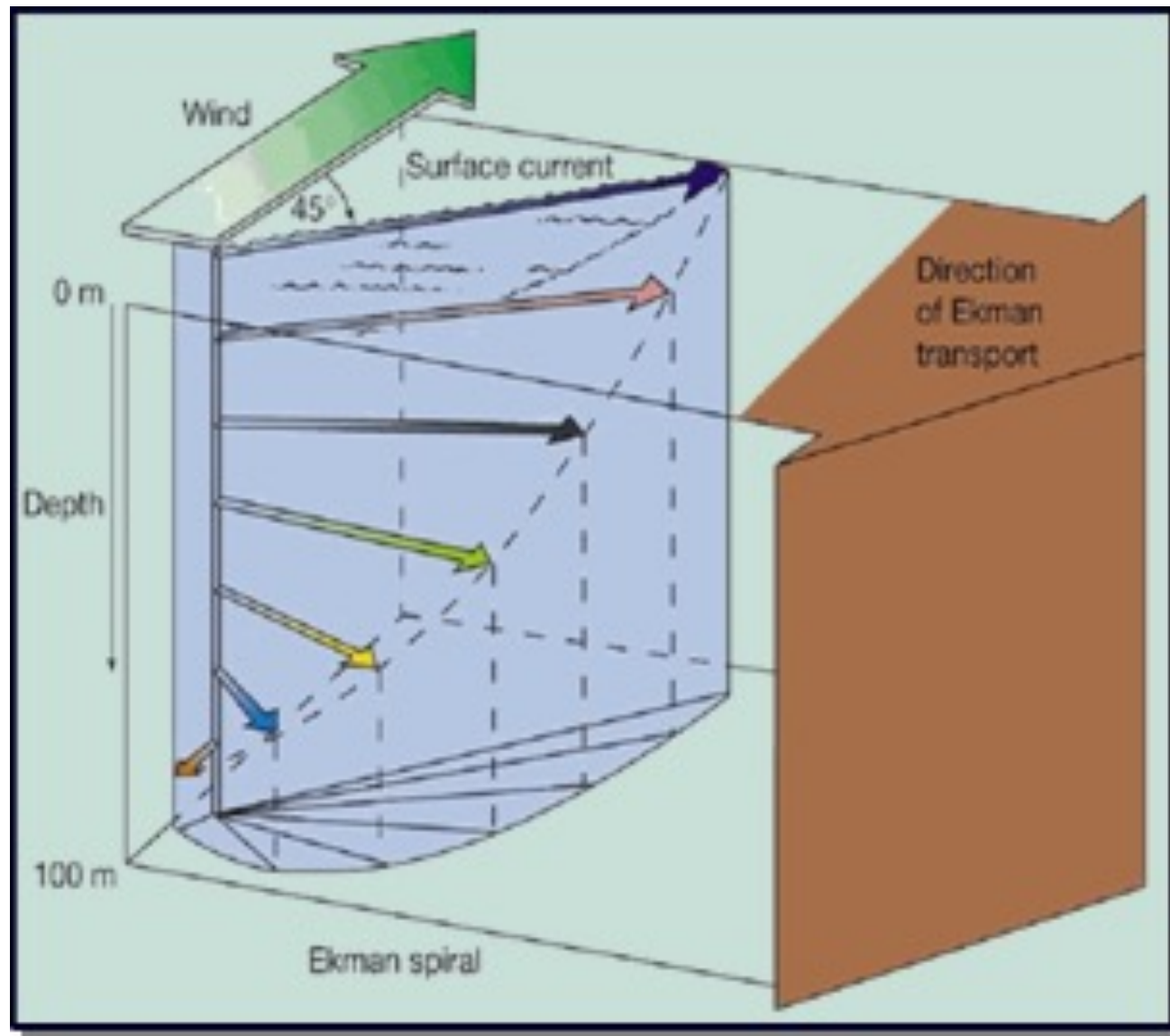
1+2+3 = Wind-Driven Circulation



# Frictional Shearing Stress + Rotation: Ekman Spiral



## Frictional Shearing Stress + Rotation: Mass Transport:



Movie Excerpts from

1957/58 Station Alpha Drift

# Beaufort Sea 1958 --> First observed Ekman Spiral

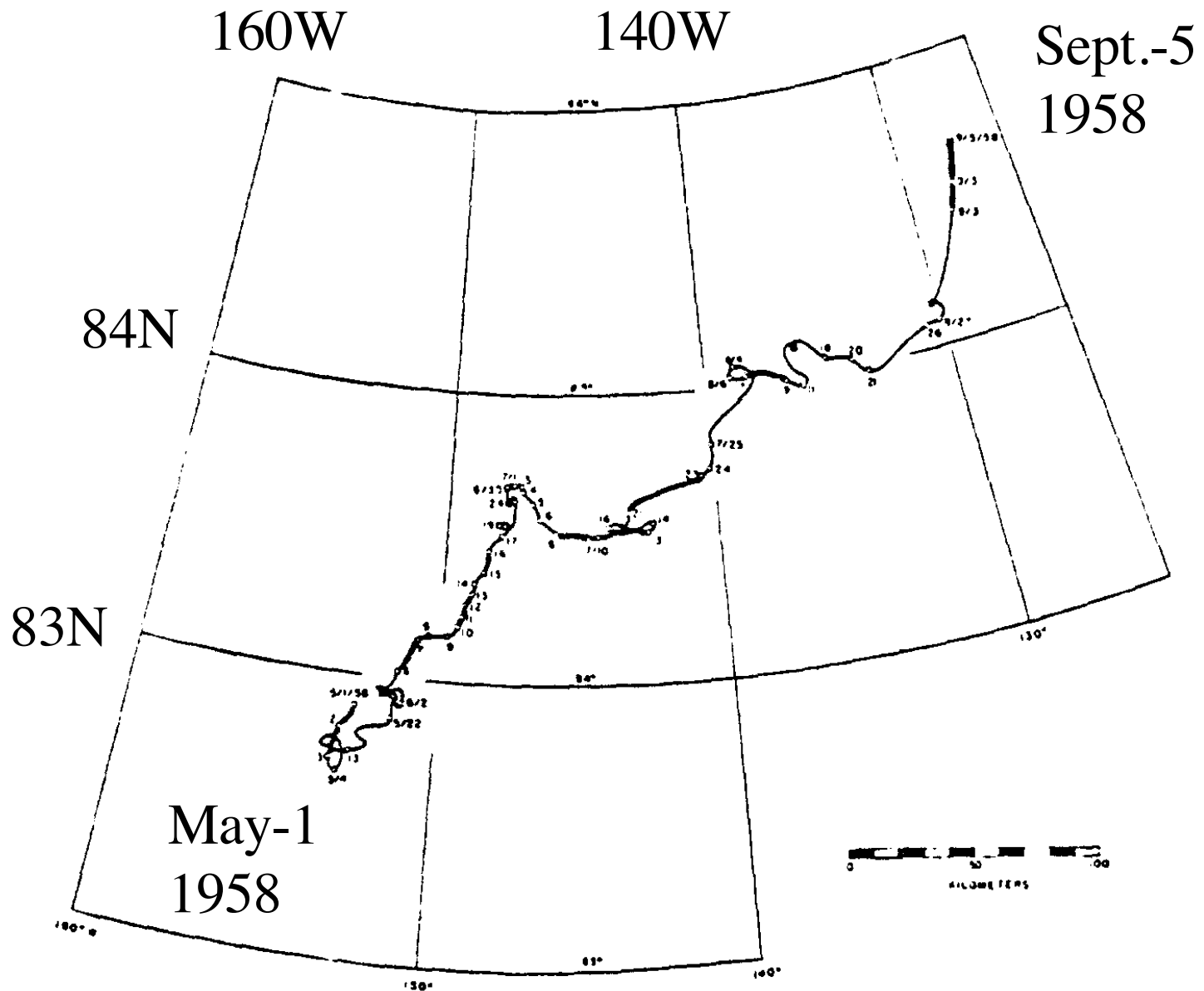


Fig. 1. Drift track of Station Alpha between 5/1/58 and 9/5/58. Barred lines indicate periods of equilibrium drift.

Hunkins (1966)

# Beaufort Sea 1958 --> First observed Ekman Spiral

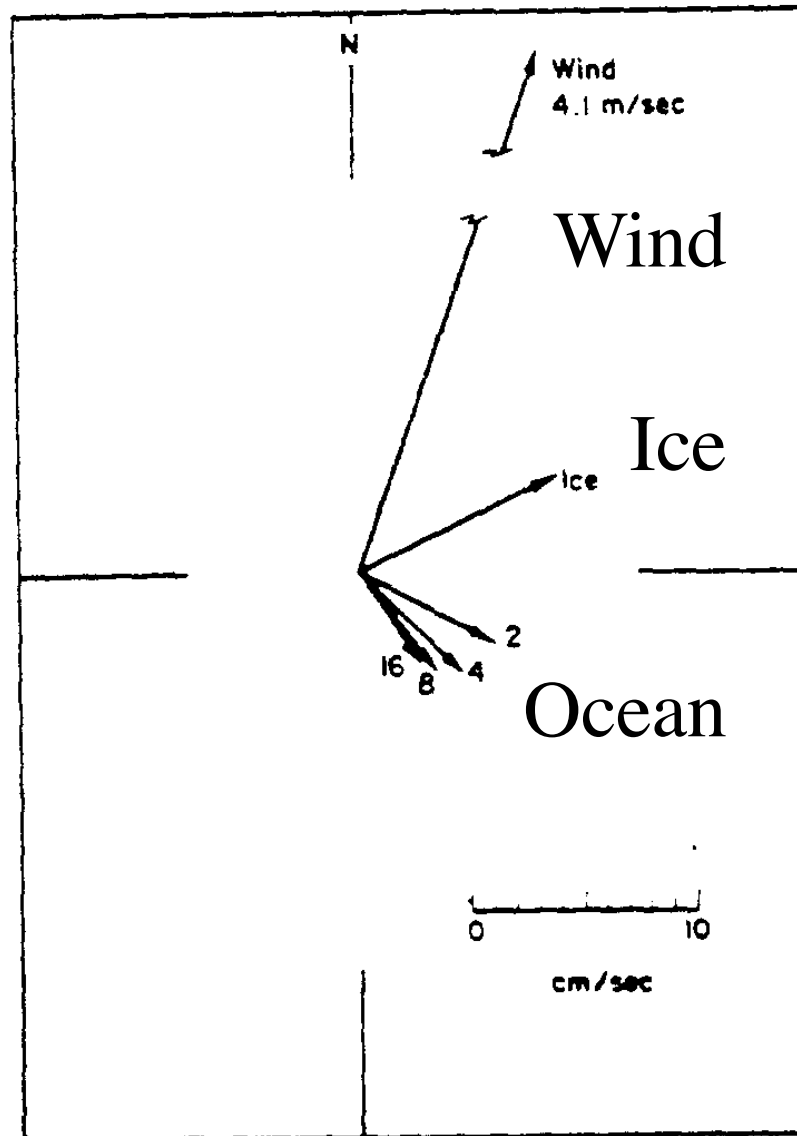


Fig. 6. Mean current hodograph for drift equilibrium periods 8-13. Numbers refer to depths in meters below the base of the ice.

# Beaufort Sea 1958 --> First observed Ekman Spiral

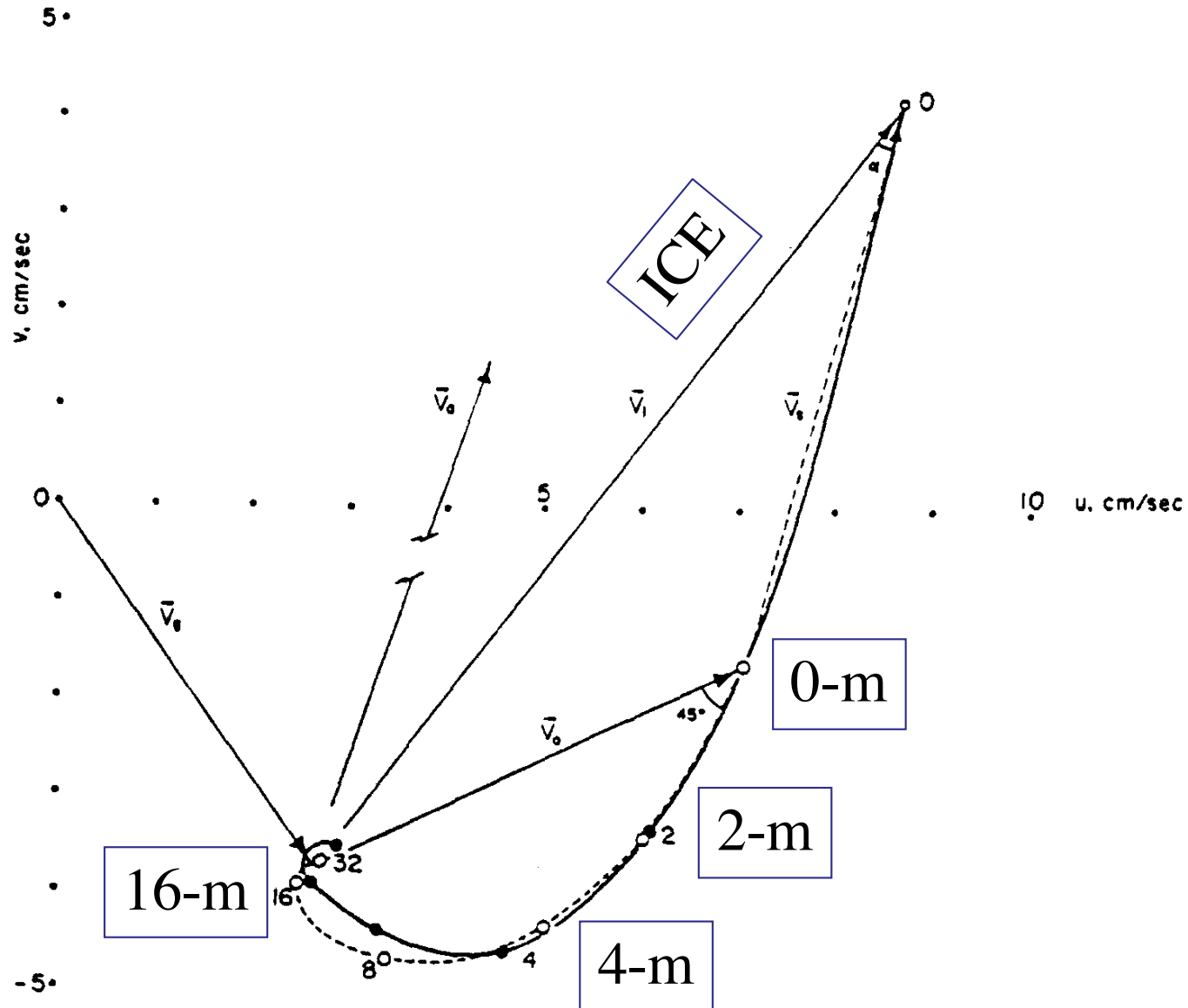
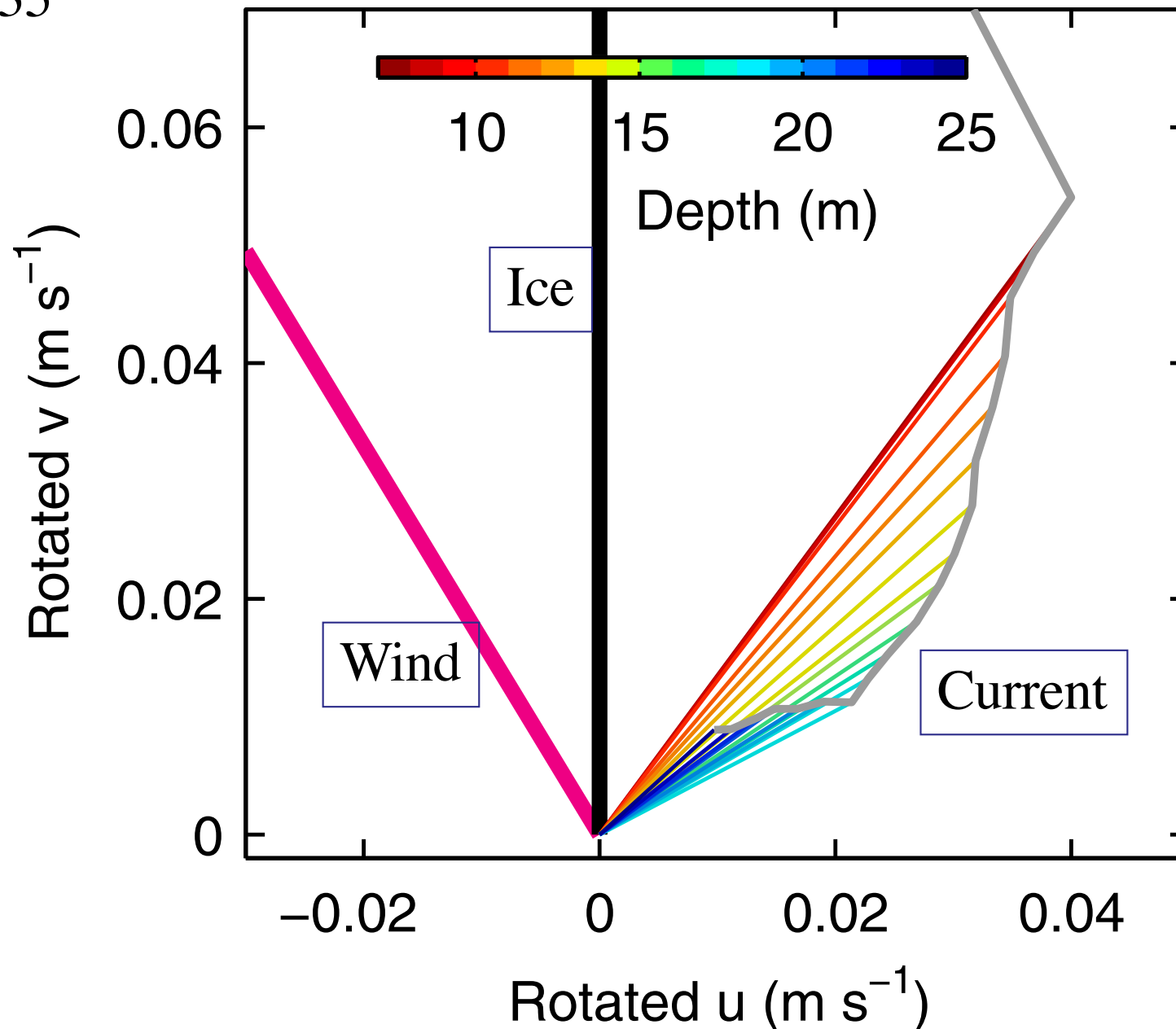


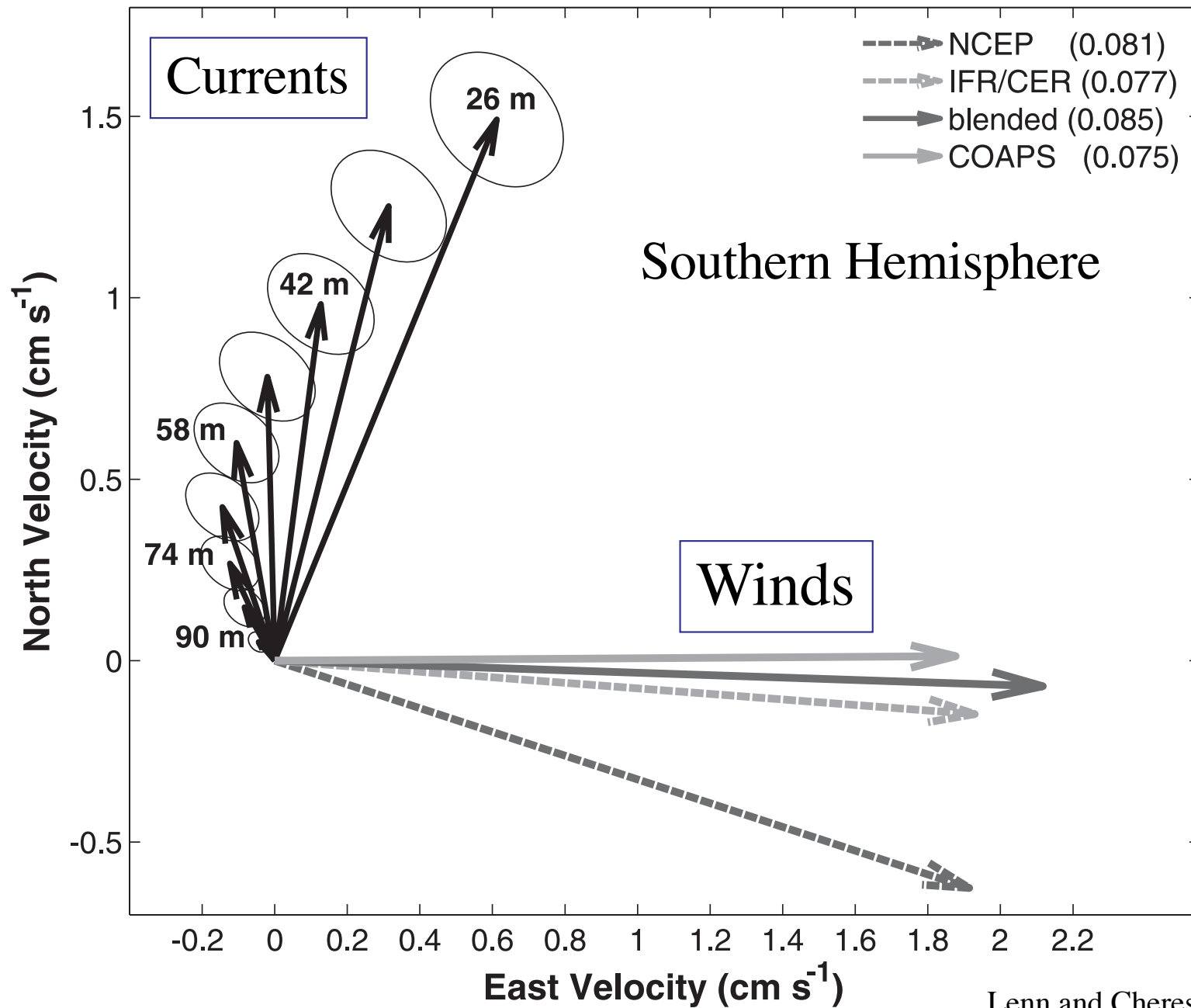
Fig. 7. Comparison between mean observed hodograph for periods 8-13 (solid line and circles) and theoretical curve for surface boundary layer and Ekman layer with  $D \approx 18$  m (dotted line and open circles). Numbers refer to depths in meters below the base of the ice.

Beaufort Sea 2009 --> Modern Ekman Spiral Observations  
Northern Hemisphere

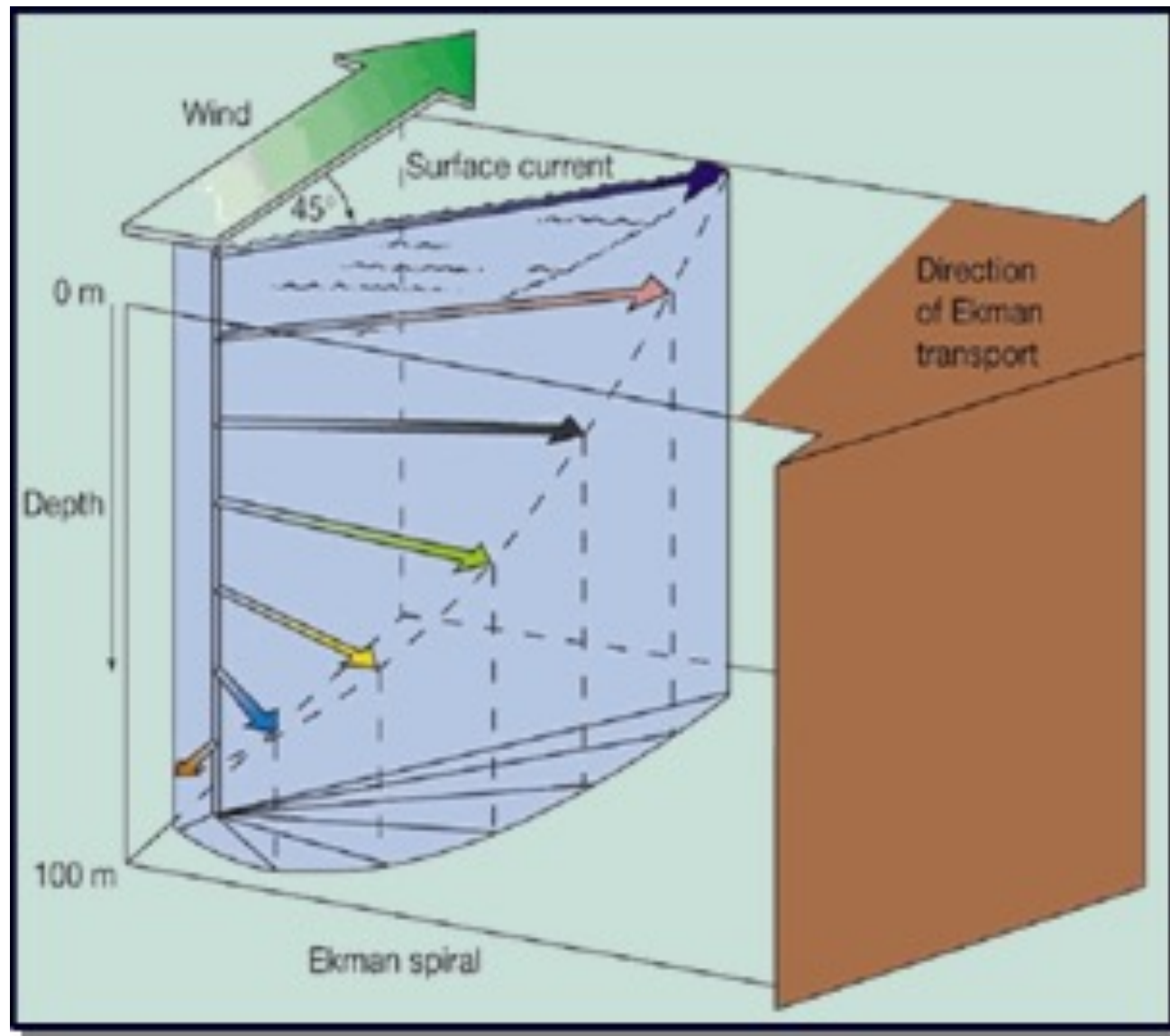
ITP-35



# Drake Passage 2004 --> Modern Ekman Spiral Observations



## Frictional Shearing Stress + Rotation: Mass Transport:



Poll12\_1:

How does the wind stress  
create pressure gradients?

# How to create a High pressure center in the the ocean?

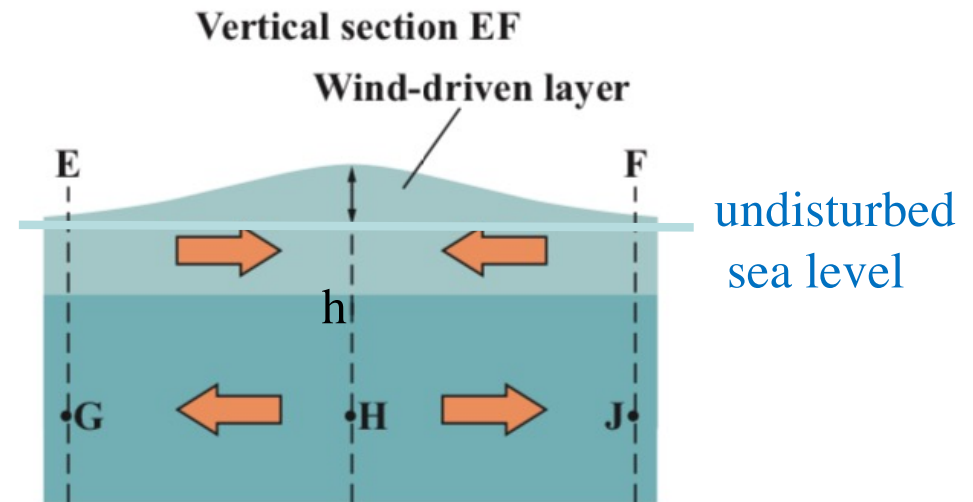
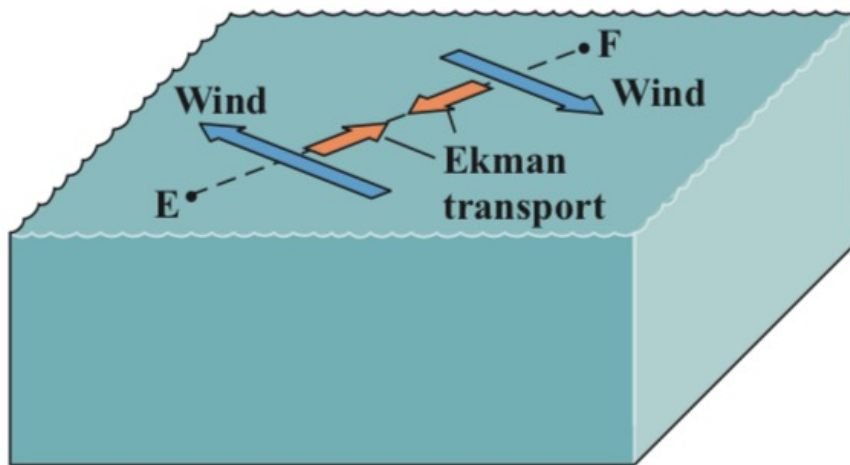
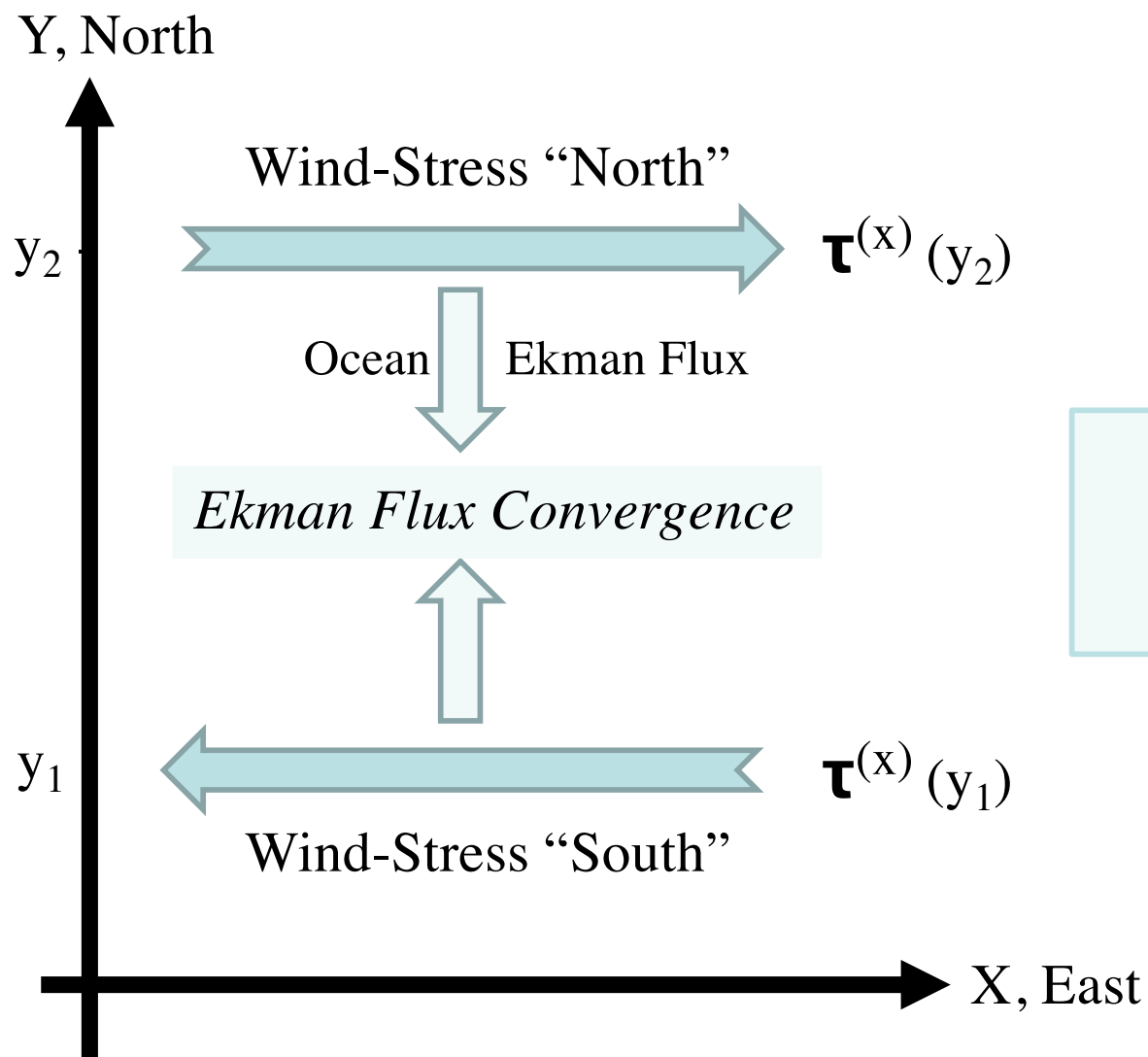


Fig. 8.5

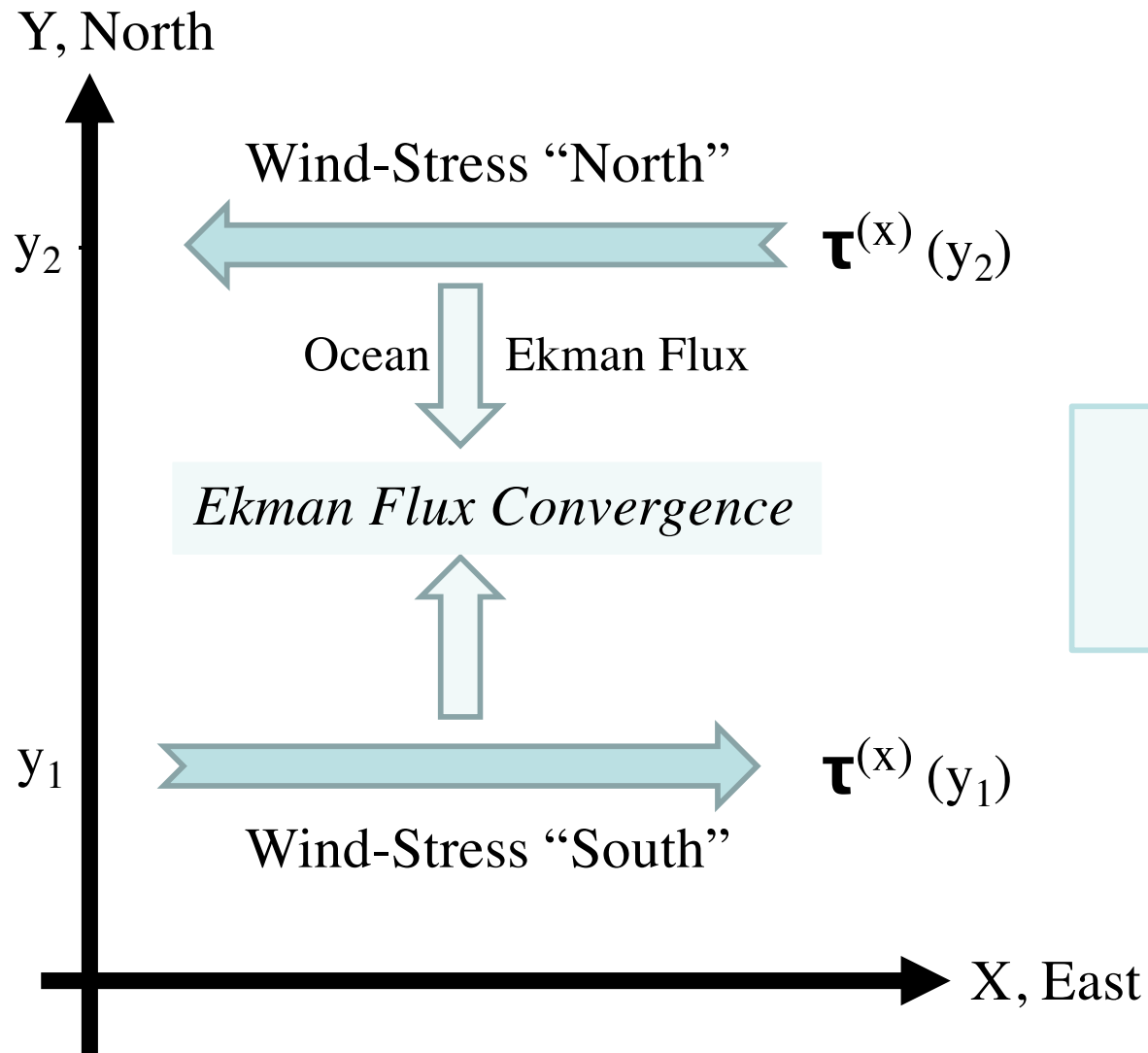
$$\begin{aligned}
 \text{pressure @H} &= \text{pressure @G} + \\
 &\rho * g * h \\
 &= \text{pressure @J} \\
 &+ \rho * g * h
 \end{aligned}$$

$\rho$  is ocean density ( $\text{kg/m}^3$ )  
 $g$  is constant of gravity ( $\text{m/s}^2$ )



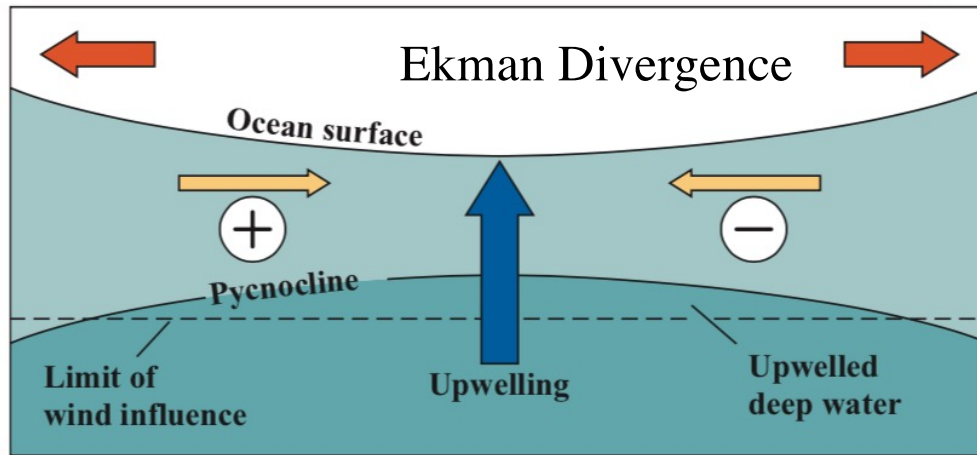
## Ekman Pumping North of Equator

Downwelling

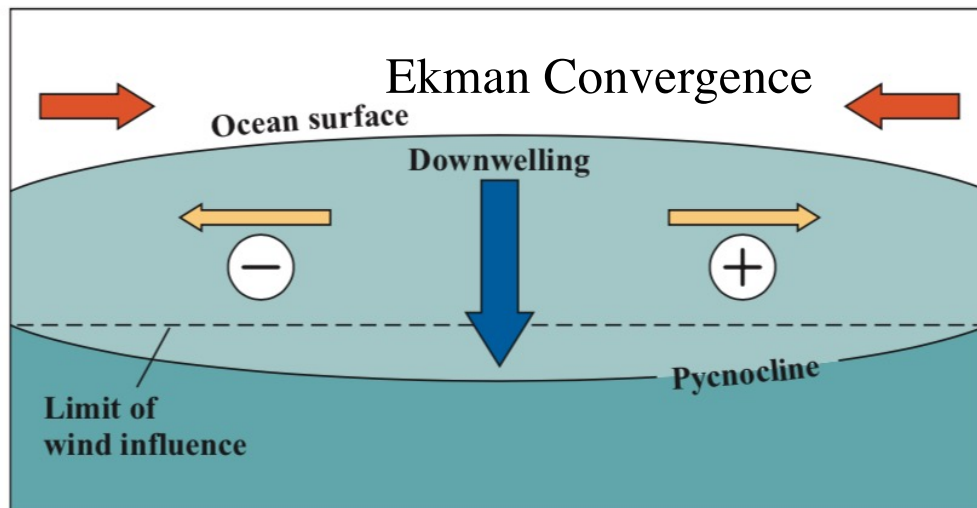


## Ekman Pumping South of Equator





(a) Divergence



(b) Convergence

## 1. Divergent Ekman Transport

## 2. Low Pressure Center

## 3. Geostrophic Circulation

“+” into page, “-” out of page

## 4. Upwelling (Ekman Pumping)

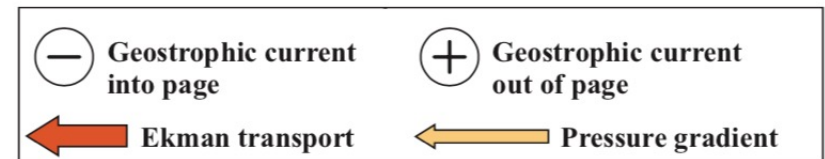
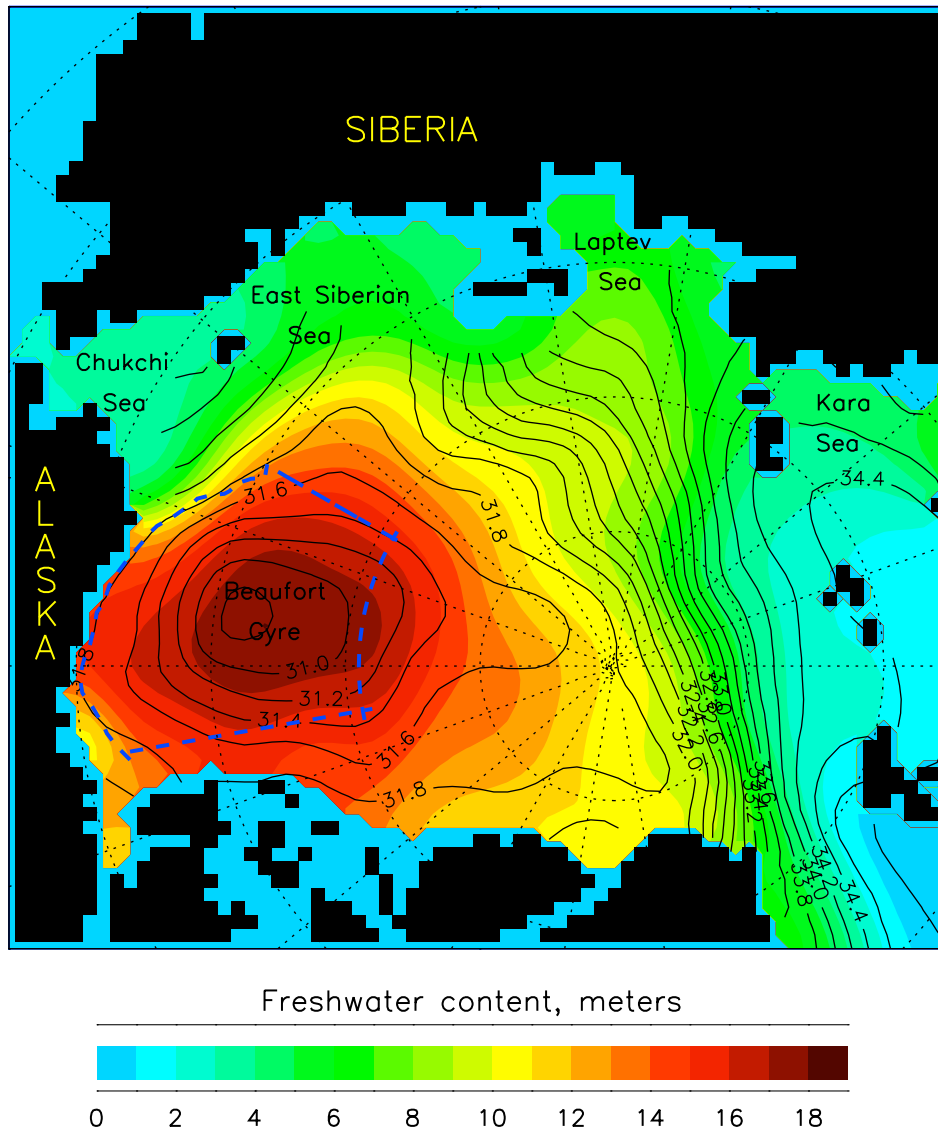


Fig. 8.1

# Arctic Ocean Freshwater Content

Why is it there?

What does it do?



**Figure 1.** Climatology of freshwater content in the Arctic Basin (shown in colors). Solid lines depict mean 1950–1980 salinity at 50 m. Freshwater content is calculated relative to salinity 34.8 on the basis of 1950–1980 data from *Timokhov and Tanis* [1998] averaged for all decades. The Beaufort Gyre Region (BGR) is bounded by thick dashed blue lines.

Shearing Stress  
+  
Rotation  
+  
Time Dependence:

Observations

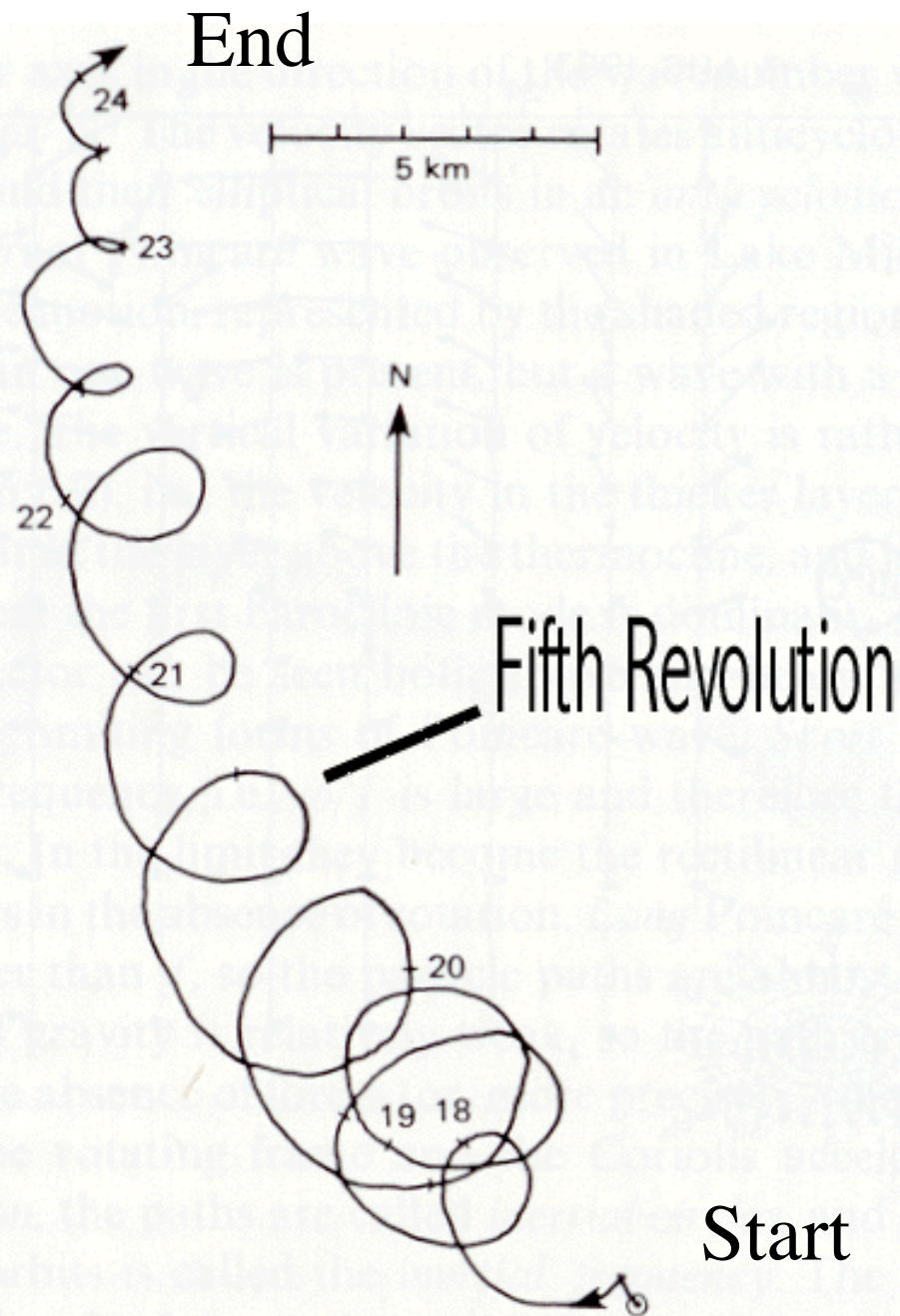


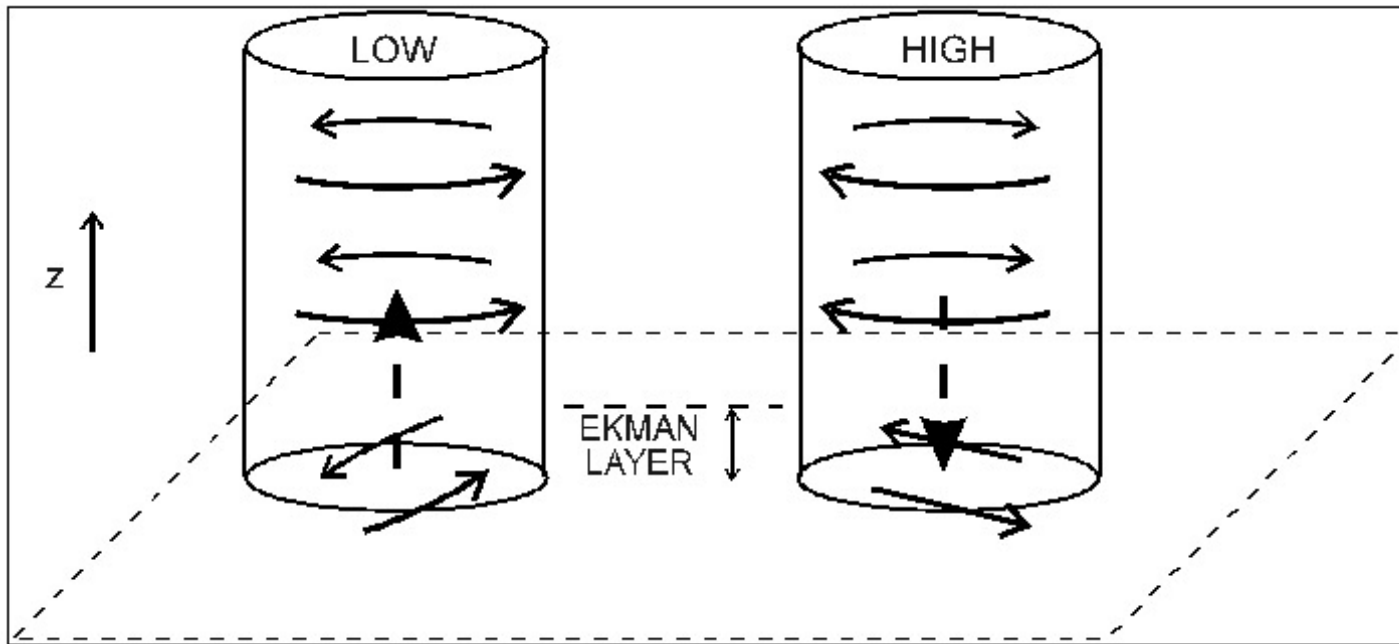
Fig. 8.3. The historic current measurements in the Baltic by Gustafson and Kullenberg (1936), showing oscillations of near-inertial period. The plot is a progressive vector diagram, showing the displacement a particle would have, given the velocity observed at the current meter. 1

Adapted from Gill (1982)

cyclonic

anti-cyclonic

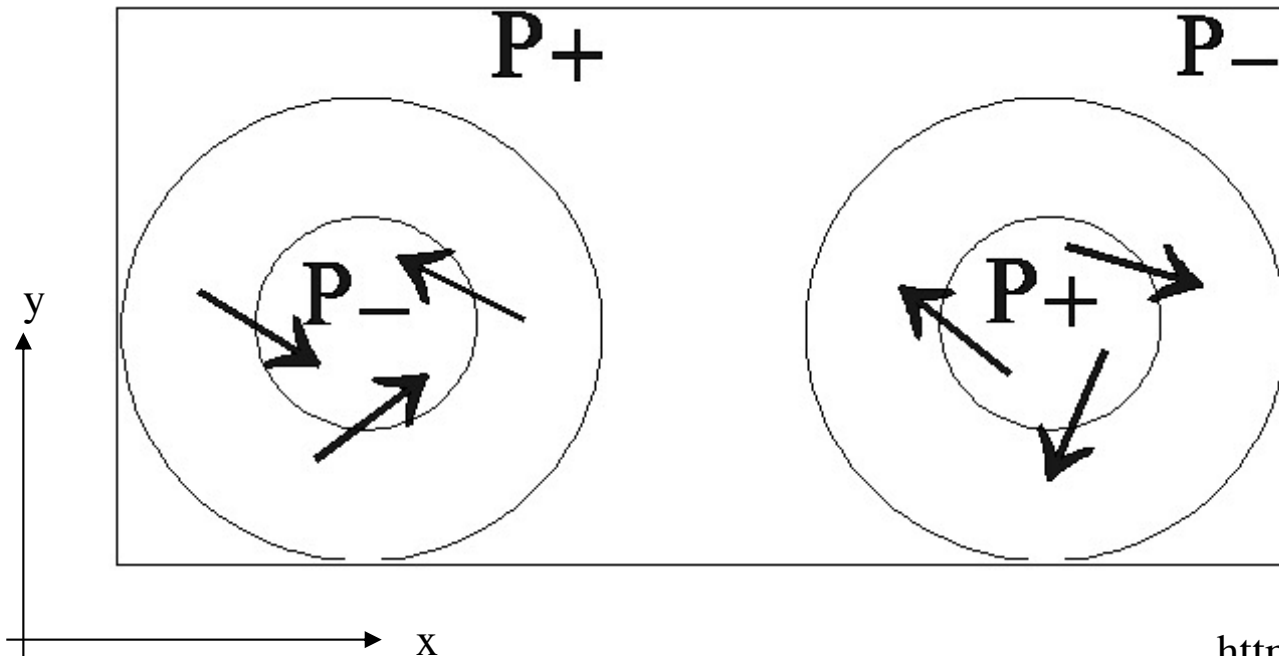
geostrophic  
circulation with  
relative vorticity



leads to

$P_+$

$P_-$



frictional boundary  
layer flow from  
high to low pressure

→ divergence!!!  
→ vertical velocity