

# MAST 4667/667: Introduction to Arctic Oceanography (Fall 2014)

Oct.-16, 2014

## Workshop/Homework-7: Thermal Wind (PhD-students only)

Data: Ice-Tethered Profiler (ITP) at <http://www.whoi.edu/website/itp/overview>

**Introduction.** \* Observed vertical and horizontal density gradient relate to a geostrophic flow field via the thermal wind relation

$$\partial V / \partial z = -g / (\rho f) \partial \rho / \partial x$$

where  $V$  is the velocity component perpendicular to the two stations at  $x_1$  and  $x_2$  from which to estimate  $\partial \rho / \partial x \approx (\rho_2 - \rho_1) / (x_2 - x_1)$ . The constants  $g = 9.81 \text{ m/s}^2$  and  $f = 1.4 \times 10^{-4} \text{ s}^{-1}$  are gravity and Coriolis parameters. The vertical co-ordinate  $z$  increases towards the sea surface and  $x$  is an along-track distance.

Estimating  $V$ , you must perform a vertical integral of the right-hand side of the thermal wind equation. Start this integration with  $V(z = -700) = 0 \text{ m/s}$ .

**Goal.** Estimate geostrophic flows using ITP buoy data.

### Assignment.

1. Generate a clean, averaged time series of density profiles 5 days apart.
2. Estimate the vertical current shear  $\partial V / \partial z$  as a function of time  $t$ , depth  $z$ , and along-track distance  $x$  from your observations of  $\rho = \rho(t, x(t), z)$ .
3. For successive locations 10 days apart, estimate the velocity  $V(t, x(t), z)$  relative to zero flow at 700-m depth that serves as the assumed level of no motion.
4. Show the geostrophic velocity both as a section, e.g.,  $V(x, z)$  and as a map, e.g.,  $V(\text{lat}, \text{lon}, z = -10 \text{ m})$ . Recall that  $V$  is perpendicular to a line connecting the two profile locations  $x_1$  and  $x_2$  that in your data may change with time also.
5. What is the difference between the geostrophic velocity near the surface  $V(t, x(t), z = -10 \text{ m})$  and the observed buoy drift (or ice) velocity?
6. Post graphics and data on your web-pages along with an interpretation as a separate text file not to exceed 500 words.

(\*) This way to estimate thermal wind shear is for instructional purposes only. Alternative approaches involve production of a grid  $\rho_{ij} = \rho(x_i, z_j)$  which is then shifted in "i" and summed in "j." There are many ways to generate and manipulate grids.